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LON-CAPA Mathematical Functionality

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LON-CAPA Mathematics

- Mathematics Output:
 - typesetting
 - graphing
- Generating Mathematics Problems:
 - symbolic math functionality
 - statistics packages
- Mathematics Input:
 - numerical
 - formula evaluation
 - sampling
 - symbolically
 - checking for properties
 - graphical input
 - bubble sheets
 - clickers







Today's presentation is going to show some very specialized functionality. Because you can does not mean you have to.



• Typesetting:

The solution is

LaTeX can be embedded anywhere in the material

$$x_{1,2} = -\frac{p}{2} \pm \sqrt{\left(\frac{p}{2}\right)^2 - q}$$

• Editor for non-native LaTeX speakers

Text Block Delete?	🗧 Edit Math 🕐	Greek Symbols 🔞			
Rich formatting » File Edit Options Help The solution is Image: Colspan="3">Image: Colspan="3" Image:					
		 det Tr			
42 $\int_{0}^{42} \times d$					



 Generated on-the-fly, can vary from student to student.

	Script	Delete?
	\$k=&random(2,5	,1)
nse	ert:	\$
	Text Block De	lete? 🗧 🗧 Edit Math 🕐
	<u>Rich formatting</u>	<u>»</u>
	What is the de <m eval="on">\ with respect t</m>	erivative of [\frac{1}{\$k}x^\$k\] :o <m>\$x\$</m> ?

What is the derivative of	$\frac{1}{3}x^3$
What is the derivative of	$\frac{1}{2}$ m 5
with respect to x ?	520



- <algebra>-tag to pretty-print the output from computer algebra systems
- Example: \$formula="a*x^5"

Text Block	Delete?	•	Edit Math)	
<u>Rich formatting</u>	<u>»</u>				
What is the de	erivative of <	algebra>\$fo	rmula <td>> with respect</td> <td>to x?</td>	> with respect	to x?
What is the	derivative o	ofa∙x ⁵ witi ries 0	h respect to	o x?	

- One-source, multiple target
- Looks good in print
 - Online: The solution is

$$x_{1,2} = -\frac{p}{2} \pm \sqrt{\left(\frac{p}{2}\right)^2 - q}$$

• Print (dynamically generated PDF):

The solution is

$$x_{1,2}=-rac{p}{2}\pm\sqrt{\left(rac{p}{2}
ight)^2-q}$$



- Dynamic Graphing
 - Data-Points
 - Functions
 - Line-Graphics
- Internally uses
 GNUplot



.

Dete peinte	Curve Delete?
 Data points 	Color of curve (x000000) x000000
50	Name of curve to appear in key
45	Plot with: points 🔷
40	Line width (may not apply to all plot styles) 1 🔷
35	Line type (may not apply to all plot styles) solid
30	Point type (may not apply to all plot styles) 3
25	Point size (may not apply to all plot styles) 2
 20	Point to fill for filledcurves closed
15 ····································	Comma or space deliminated curve data
	@x
5 0 0 5 10 15	Insert:
	Comma or space deliminated curve data
	@y
	Insert:



Data points



Functions





• Line graphics



Generating Mathematics Problems

- LON-CAPA problems include
 - Perl Scripting Environment
 - MAXIMA Computer Algebra System
 - R Statistics Package
- Problems not just randomized, but randomly generated with desired properties







Generating Mathematics Problems

 Direct calls to MAXIMA: \$result=&cas('maxima',\$expression);

• Simple example: use computer algebra system to calculate a reduced fraction

Script

Delete?

Construct an Egyptian Fraction that can be represented by three terms with denominators between 3 and 12 @denominators=(&random_permutation(&random(1,1000,1),(3..12)))[0..2]; \$egyptian='1/'.(join('+1/',sort{\$a<=>\$b}(@denominators))); \$possible="A possible solution is \$egyptian";

<pre># Let the CAS figure out the value \$solution=&cas('maxima',\$egyptian);</pre>	Write 103/165 as an Egyptian Fraction	
	Submit Answer Tries 0	
	Answer for Part: 0 A possible solution is 1/3+1/5+1/11	

Generating Mathematics Problems

• Direct calls to R:

\$result=&cas('R',\$expression);

\$results=&cas_hashref('R',\$expression);

• Example: generate a distribution with certain properties:

 Script
 Delete?

 \$seed=&random(1,500,1);

 \$n=&random(15,25,1);

 \$offset=&random(2,5,0.1);

 \$slope=&random(0.6,2.5,0.1);

 # construct a data set using R

 # dump is for debugging, print to screen to see data structure

 (\$data,\$dump)=&cas_hashref('R', "set.seed(\$seed);x<-1:\$n;w<-1+sqrt(x)/2;data.frame(x=x,y=\$offset+\$slope*x+rnorm(x)*w);");</td>

 @x=&cas_hashref_array(\$data,'x');

 @y=&cas_hashref_array(\$data,'y');

	Script Delete?	
	<pre>\$vx=&random(3,6,0.1); \$vy=&random(2,8,0.1); \$vz=&random(4,10,0.1); \$t=&random(4,0.1);</pre>	An object starts at the origin with a constant velocity of
	<pre>@solution=(\$vx*\$t,\$vy*\$t,\$vz*\$t);</pre>	→ (4.4) m
Insei	t	v = 2.5 - 7.2 s
	Text Block Delete?	Where is it 4 seconds later? 17.6,10,28.8 m
	<u>Rich formatting »</u>	
	An object starts at the origin with a co <m eval="on"> \[\vec{v}=\left(\begin{array}{c}\$vx\\ \$v \frac{\mbox{m}}{\mbox{s}}\] </m> Where is it \$t seconds later?	<pre>onstant velocity of vy\\ \$vz\end{array}\right) Simplest input: numerical</pre>
	Check Spelling	пипенса
Insei	t	•
Res	oonse: Numerical Delete?	♦ Insert:
Ans		



	Mathematics Input Script Delete? = \$k=&random(3,6,1); \$formula="a*x^\$k";
	<pre>\$m=\$K-1; \$derivative="\$k*a*x^\$m";</pre>
What is t	he derivative of $a \cdot x^4$ with respect to x?
Subm	it Answer Tries 0
Answer	for Part: 0 4*a*x^3
	What is the derivative of <algebra>\$formula</algebra> with respect to x?
	Check Spelling
	rt:
	Response: Formula Delete? 🔷 Insert:
	Answer: \$derivative Sample Points:
	 Symbolically: exactly one exact answer (but equivalent forms)



- Checking properties
 - Using R:

Provide a list of 3 numbers (separated by commas) that has a mean value of 6.2.

Resp	onse: Math	Delete?	Insert:]
String	to display for answe raries:	er: [\$answer])		Algebra System: R
	Answer algorithm			Delete?	\
	x<-c(RESPONSE[1], abs(mean(x)-LONCA	,RESPONSE[2],RESP APALIST[1])<0.001	ONSE[3]);		



Checking properties
 Using MAXIMA:

Give an example of a function

1. which is orthogonal to

 $-2 \cdot \cos(5 \cdot x) + 2 \cdot \sin(4 \cdot x)$

with respect to the scalar product

Tri

 $\langle g \mid h \rangle = \cdot \int_{-\pi}^{\pi} dx g(x) \cdot h(x)$

2. whose norm is 1.

Submit Answer

Answer algorithm

overlap:integrate((RESPONSE[1])*(LONCAPALIST[1]),x,-%pi,%pi)/%pi; norm:integrate((RESPONSE[1])*(RESPONSE[1]),x,-%pi,%pi)/%pi; is(overlap=0 and norm=1);







At t=0 s, a car cruises at a constant positive velocity. Suddenly, a light switches to red. At t=10 s, the driver is maximum on the brake. The car then stops in front of the red light for over 2 seconds. Eventually, it drives off, and then again cruises at a constant velocity. The car cannot accelerate with more than 3 m/s^2 . Provide a graph of its acceleration as a function of time.





- Problems can also be rendered for bubble sheets
- Every student gets a different version

A crate with a mass of 177.5 kg is suspended from the end of a uniform boom with mass of 88.5 kg. The upper end of the boom is supported by a cable attached to the wall and the lower end by a pivot (marked X) on the same wall. Calculate the tension in the cable.



1 pt A crate with a mass of 177.5 kg is suspended from the end of a uniform boom with mass of 88.5 kg. The upper end of the boom is supported by a cable attached to the wall and the lower end by a pivot (marked X) on the same wall. Calculate the tension in the cable.





CODE - AACHDA LB 271 - Introductory Physics Lecture Version A

Name:

LB271 Fall 2009 Final Exam Version A

Gravitational Accellera- tion on Earth	$g = 9.81 m/s^2$
Gravitational Constant	$G = 6.67 \cdot 10^{-11} m^3 / (kg \cdot s^2)$
Absolute Zero	-273.15°C
Gas Constant	$R = 8.31 J/(K \cdot mol)$
Boltzmann Constant	$k = 1.38 \cdot 10^{-23} J/K$
Avogadro's number	$N_A = 6.02 \cdot 10^{23}$ parti- cles/mol
Specific heat of water va- por	$c_{\text{vapor}} = 0.48 k cal/(kg \cdot K)$
Specific heat of liquid wa- ter	$c_{water} = 1kcal/(kg \cdot K)$ = 4186J/(kg · K)
Specific heat of water ice	$c_{ice} = 0.5kcal/(kg \cdot K)$
Latent heat of fusion for water	$L_{\rm f} = 80 k cal/kg$
Latent heat of vaporiza- tionfor water	$L_V = 540 kcal/kg$



A block is being held in place on an incline. The magnitude of the force applied by the hand on the block is the same in the left and the right scenarios.

1 pt In which scenario does the incline exert a lower normal force on the block?

1. A The left scenario. B() The right scenario. C Same in both scenarios.

1 pt In which scenario does the incline exert a lower frictional force on the block?

2. A O The left scenario. B() The right scenario. C() Same in both scenarios.

1 pt By how many decibels does the sound intensity from a point source decrease if you increase the distance to it by a factor 6? 3A() 12.2 B() 13.8 C() 15.6 D() 17.6 EO 19.9 FO 22.5 GO 25.4 HO 28.7



A particle is located at x=2.0 mm and has a kinetic energy of 29.5 Joule. What is the maximum x-coordinate the particle could reach? (in mm)

4.A() 0.1 B() 0.7 C() 1.6 D() 2.6 EO 3.2 FO 4.7 GO 5.3 HO 7.6



Deep Space Nine sees Enterprise and a shuttle approach from exactly opposite directions with 0.8 c and 0.5 c, respectively. 1 pt At what fraction of the speed of light (β) does Enterprise see the shuttle approach?

5.A() 0.00 B() 0.50 C() 0.83 D() 0.91 E() 0.93 F() 1.00 G() 1.25 H() 1.30

1 pt The shuttle has a length of 9 meters when at rest. How long is it in the system of Deep Space 9? (in m) 6.A 1.8 B 2.6 C 3.7 D 5.4 EO 7.8 FO 11.3 GO 16.4 HO 23.8

1 pt Captain Picard on the Enterprise takes a 49 minute tea break. How long is this break in the system of Deep Space 9? (in min)

7.A 27 B 33 C 42 D 52 E() 65 F() 82 G() 102 H() 128

CODE - AACHDA LB 271 - Introductory Physics Lecture Version A

1 pt You have two organ pipes of the same length, one closed at both ends, one half open. Which one has a lower fundamental frequency?

- B() Same.
- C() The half-open pipe.

1 pt In a very simple model of the lower atmosphere, air has a constant density of 1.26 kg/m³. How much would the air pressure change over a height difference of 130 m? (in Pa)

9.A○ 986 **B**○ 1110 **C**○ 1260 **D**○ 1420 E() 1610 F() 1820 G() 2050 H() 2320





A car drives in the forward (positive) direction. It first has a constant speed, then drives into a parking spot, waits for a few moments, and then drives out again backwards. Which one of the acceleration graphs could describe this scenario?

- 10. A Scenario A
- B Scenario B CO Scenario C
- D Scenario D
- EO None of the above.

1 pt A box is sliding uphill as shown. What is the

direction of the frictional force on the box? **11**. **A** ∩ Downhill.



 \mathbf{D} None of the above.



An object is rotating on a circular trajectory as shown. The indicated direction A is toward the center of the trajectory, C is tangential to the trajectory. The object is rotating clockwise and slowing down. 1 pt What could be the direction of the (linear) acceleration

- 12. A ODirection A. BO Direction B. CO Direction C. DO Into the paper.
 - E() Out of the paper.

1 pt What could be the direction of the angular accelera-

13. A Direction A. BO Direction B. C Direction C. D) Into the paper. EO Out of the paper.

1 pt

You have two identical looking spools (same mass, same shape, same size). However, one is hollow, made from iron, the other is solid, made from aluminum. A string is wound around each spool. If you pull on both strings with equal forces, which spool is going to



have the larger angular acceleration?

14. A Same B ∩ The solid spool CO The hollow spool





CODE - AAFIHH LB 271 - Introductory Physics Lecture Version A

Name:

LB271 Fall 2009 Final Exam Version A

Gravitational Accellera- tion on Earth	$g = 9.81 m/s^2$
Gravitational Constant	$G = 6.67 \cdot 10^{-11} m^3 / (kg \cdot s^2)$
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Specific heat of water ice	$c_{ice} = 0.5 k cal/(kg \cdot K)$
Latent heat of fusion for water	$L_{\rm f} = 80 k cal/kg$
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A block is being held in place on an incline. The magnitude of the force applied by the hand on the block is the same in the left and the right scenarios.

1 pt In which scenario does the incline exert a higher frictional force on the block?

1. A O The left scenario. B() The right scenario. C() Same in both scenarios.

1 pt In which scenario does the incline exert a higher normal force on the block?

2. A O The left scenario. B() The right scenario. CO Same in both scenarios.

1 pt By how many decibels does the sound intensity from a point source decrease if you increase the distance to it by a factor 6? 3A() 7.10 B() 8.31 C() 9.72 D() 11.4 EO 13.3 FO 15.6 GO 18.2 HO 21.3



A particle is located at x=5.5 mm and has a kinetic energy of 9.8 Joule. What is the minimum x-coordinate the particle could reach? (in mm)

4.A 1.6 B 2.6 C 2.7 D 2.9 E() 3.0 F() 3.8 G() 5.2 H() 6.9

Deep Space Nine sees Enterprise and a shuttle approach from exactly opposite directions with 0.8 c and 0.4 c, respectively. 1 pt At what fraction of the speed of light (β) does Enterprise see the shuttle approach?

5.A() 0.00 B() 0.47 C() 0.50 D() 0.59 E() 0.78 F() 0.91 G() 1.00 H() 1.20

1 pt The shuttle has a length of 12 meters when at rest. How long is it in the system of Deep Space 9? (in m) 6.A() 3.6 B() 4.5 C() 5.6 D() 7.0 E() 8.8 F() 11.0 G() 13.7 H() 17.2

1 pt Captain Picard on the Enterprise takes a 35 minute tea break. How long is this break in the system of Deep Space 9? (in min) **7.A** \bigcirc 19 **B** \bigcirc 28 **C** \bigcirc 40 **D** \bigcirc 58

E() 85 F() 123 G() 178 H() 258

CODE - AAFIHH LB 271 - Introductory Physics Lecture Version A

1 pt You have two organ pipes of the same length, one closed at both ends, one half open. Which one has a lower fundamental frequency?

- 8. A () Same.
- B() The closed pipe.
- C() The half-open pipe.

1 pt In a very simple model of the lower atmosphere, air has a constant density of 1.22 kg/m³. How much would the air pressure change over a height difference of 110 m? (in Pa)

9A \bigcirc 1320 **B** \bigcirc 1490 **C** \bigcirc 1680 **D** \bigcirc 1900 E() 2150 F() 2430 G() 2740 H() 3100





A car drives in the forward (positive) direction. It first has a constant speed, then drives into a parking spot, waits for a few moments, and then drives out again backwards. Which one of the acceleration graphs could describe this scenario?

- 10. A O Scenario A
- B() Scenario B
- CO Scenario C D Scenario D
- EO None of the above.

1 pt A box is sliding uphill as shown. What is the direction of the frictional force on the box?

11. A OPerpendicular to the surface.

- BO Downhill.
- CO Uphill.
- $\mathbf{D} \bigcirc$ None of the above.



An object is rotating on a circular trajectory as shown. The indicated direction A is toward the center of the trajectory, C is tangential to the trajectory. The object is rotating clockwise and slowing down. 1 pt What could be the direction of the (linear) acceleration

- 12. A ODirection A. **B** Direction B. C() Direction C.
 - D() Into the paper.
 - E() Out of the paper.

1 pt What could be the direction of the angular accelera-

13. A ODirection A. BO Direction B. CO Direction C. DO Into the paper. E() Out of the paper.

You have two identi-

1 pt

cal looking spools (same mass, same shape, same size). However, one is hollow, made from iron, the other is solid, made from aluminum. A string is wound around each spool. If you pull on both strings with equal forces. which spool is going to have the larger angular acceleration?



14. A The solid spool **B**O The hollow spool C() Same









LON-CAPA can evaluate clicker data after lecture

000	LON-CAPA Change Preferences		\bigcirc		
🖕 🚽 🥑 🙆 🏠	🖳 http://phy1.lbs.msu.edu/adm/p 🔻 🕨	G • Google	Q *		
Getting Started Latest Headlin	es 🔊				
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Main Menu	Launch Remote Control	Roles	Help Exit		
Change Prefere	nces	<u>Gerd Th</u> No Role, Cumula	<u>e Kortemeyer</u> tive Privileges		
Menu->Set User Preferences->Register Clicker Change Preferences					
Enter response device ("click	ker") numbers				
005BC59E					
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Main Menu	Return to Last Location	Navigate Contents	
Grading (msu_8p96131ebae7b47b8msul1 ss08lbs272)			
Current Resource: Mon, Mar 10th			
Part: 0 score Type: numerical			
Specify a file containing the clicker information for this resource.			
Choose File MonMar10thA.csv			
Type: i>clicker 🛟			
 Award points just for participation 			
 Correctness determined from response by course personnel 			
Correctness determined from response with clicker ID(s)			
Percentage points for correct solution: 100			
Percentage points for incorrect solution: 60			
Upload File			



i>clicker2
 integrated
 in LON CAPA





Thank You

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